Reinforced Concrete Tilt-Up Wall Panel with Opening Analysis and Design (ACI 551)
Reinforced Concrete Tilt-Up Wall Panel with Opening Analysis and Design (ACI 551.2R-15 Provisions)

Tilt-up is a form of construction with increasing popularity owing to its flexibility and economics. Tilt-up concrete is essentially a precast concrete that is site cast instead of traditional factory cast concrete members. A structural reinforced concrete tilt-up wall panel with opening in a single-story warehouse (big-box) building provides gravity and lateral load resistance for the following applied loads from three roof joists bearing in wall pockets in addition to the wind:

- **Roof dead load** = 2.4 kip per joist
- **Roof live load** = 2.5 kip per joist
- **Wind load** = 27.2 psf

The assumed tilt-up wall panel section and reinforcement are investigated after analysis to verify suitability for the applied loads then compared with numerical analysis results obtained from spWall engineering software program from StructurePoint. Additionally, different modeling and analysis techniques using spWall engineering software program to investigate and design tilt-up wall panels with openings are discussed.

![Figure 1 – Reinforced Concrete Tilt-Up Wall Panel Geometry (with 10 x 15 ft Door Opening)](image-url)
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Code

Building Code Requirements for Structural Concrete (ACI 318-11) and Commentary (ACI 318R-11)

Reference

Design Guide for Tilt-Up Concrete Panels, ACI 551.2R-15, 2015, Example B.2

spWall Engineering Software Program Manual v5.01, STRUCTUREPOINT, 2016

Design Data

\( f' = 4,000 \text{ psi normal weight concrete} \ (w_c = 150 \text{ pcf}) \)
\( f_y = 60,000 \text{ psi} \)

Wall length = \( l_c = 31 \text{ ft} - 1.5 \text{ ft} = 29.5 \text{ ft} \)

Assumed wall thickness = 8.75 in. (Note: reference example started with a thickness of 6.25 in. that was deemed not sufficient to meet tension control condition to use alternative design method).

Assumed eccentricity = \( e_{cc} = 3 \text{ in.} \)

Assumed vertical reinforcement: 7 #6 (single layer) for the left leg (design strip)
7 #6 (single layer) for the right leg (design strip)

Solution

The effect of openings on out-of-plane bending in tilt-up panels can be approximated by a simple, one-dimensional strip analysis that provides accuracy and economy for most designs. Where openings occur, the entire lateral and axial load, including self-weight above the critical section, is distributed to supporting legs or design strips at each side of the opening (sometimes referred to as wall piers).

The effective width of the strip should be limited to approximately 12 times the panel thickness to avoid localized stress concentrations along the edge of the opening. This limit is not mandated by ACI 318, but is included as a practical guideline where the opening width is less than one-half the clear vertical span. In most cases the tributary width for loads can be taken as the width of the strip plus one-half the width of adjacent openings. Tilt-up design strips should have constant properties for the full height and the reinforcement should not be cut off just above or below the opening. Thickened vertical or horizontal sections can be introduced within the panel where openings are large or where there are deep recesses on the exterior face. Some conditions may require ties around all vertical reinforcement bars in a vertical pilaster for the full height of the tilt-up panel.
**Left Leg Analysis and Design**

Figure 2 – Tilt-Up Design Strips Tributary Widths for Loads

1. **Minimum Vertical Reinforcement**

   \[
   \rho_t = \frac{A_{v,vertical}}{b \times h} = \frac{3.08}{(4 \times 12) \times 8.75} = 0.0073
   \]

   \[ACI 318-11 (2.1)\]

   \[\rho_{min} = 0.0015\]

   \[ACI 318-11 (14.3.2)\]

   \[\rho_t = 0.0073 \geq \rho_{min} = 0.0015 \text{ (o.k.)}\]

   \[s_{t,\text{max}} = \text{smallest of } \left\{ \frac{3 \times h}{18 \text{ in.}} \right\} = \text{smallest of } \left\{ \frac{3 \times 8.75}{18 \text{ in.}} \right\} = \text{smallest of } \left\{ \frac{26.25 \text{ in.}}{18 \text{ in.}} \right\} = 18 \text{ in.}\]

   \[ACI 318-11 (7.6.5)\]

   \[s_{t,\text{provided}} = \frac{4 \times 12}{7} = 6.86 \text{ in.} \leq s_{t,\text{max}} = 18 \text{ in.} \text{ (o.k.)}\]

The design guide for tilt-up concrete panels ACI 551 states that tilt-up concrete walls can be analyzed using the provisions of Chapter 14 of the ACI 318-11. Most walls, and especially slender walls, are widely evaluated using the “Alternative design of slender walls” in Section 14.8. The same provisions are presented in ACI 318-14 but reorganized in different chapters and in slightly revised terminology. The method is applicable when the conditions summarized below are met:

- The cross section shall be constant over the height of the wall \textit{ACI 318-11 (14.8.2.2)}
- The wall can be designed as simply supported \textit{ACI 318-11 (14.8.2.1)}
- Maximum moments and deflections occurring at midspan \textit{ACI 318-11 (14.8.2.1)}
- The wall must be axially loaded \textit{ACI 318-11 (14.8.2.1)}
- The wall must be subjected to an out-of-plane uniform lateral load \textit{ACI 318-11 (14.8.2.1)}
- The wall shall be tension-controlled \textit{ACI 318-11 (14.8.2.3)}
- The reinforcement shall provide design strength greater than cracking strength \textit{ACI 318-11 (14.8.2.4)}

3. Tilt-Up Wall Structural Analysis

3.1. Applied loads

The tributary width for loads can be taken as the width of the strip plus one-half the width of adjacent openings.

\[
\text{Wall self-weight} = \frac{8.75}{12} \times 150 \times \left[ 4 \times \left( \frac{29.5}{2} + 1.5 \right) + 5 \times (31 - 15) \right] \times \frac{1 \text{ kip}}{1000 \text{ lb}} = 15.9 \text{ kip}
\]

Joist loads are divided between the individual legs assuming an equivalent simply supported beam across the top of the panel with the supports at the centerline of each leg.

- \( P_{DL} = 4.5 \text{ kip} \) (for the left leg)
- \( P_{LL} = 4.7 \text{ kip} \) (for the left leg)

\( w = 27.2 \text{ lb/ft}^2 \)

3.2. Maximum wall forces

The calculation of maximum factored wall forces in accordance with 14.8.3 including moment magnification due to second order (P-\( \Delta \)) effects is shown below (load combination \( U = 1.2 \times D \times 1.6 \times L_r \times 0.5 \times W \) is considered in this example):

\( P_{uw} = 1.2 \times 4.5 + 1.6 \times 4.7 = 12.9 \text{ kip} \)
\[ P_{um} = 12.9 + 1.2 \times 15.9 = 32.0 \text{ kip} \]

\[ w_u = 0.5 \times 27.2 \times (4 + 5) \times \frac{1 \text{ kip}}{1000 \text{ lb}} = 0.122 \text{ kip/ft} \]

\[
M_u = \frac{M_{um}}{1 - \frac{5 \times P_u \times l_c^2}{0.75 \times 48 \times E_c \times I_{cr}}}
\]

ACI 318-11 (Eq. 14-6)

\[
M_{um} = \frac{w_u \times l_c^2}{8} + \frac{P_u \times e}{2} = \frac{0.122 \times (29.5)^2}{8} + \frac{12.9 \times 3}{2 \times 12} = 14.9 \text{ ft-kip}
\]

Where \( M_{um} \) is the maximum factored moment at midheight of wall due to lateral and eccentric vertical loads, not including \( P \Delta \) effects.

ACI 318-11 (14.8.3)

\[ E_c = 57,000 \times \sqrt{f_c'} = 57,000 \times \sqrt{4,000} = 3,605,000 \text{ psi} \]

ACI 318-11 (8.5.1)

\[ I_{cr} = n \times A_{cr} \times (d - c)^2 + \frac{l_c^2 \times c^2}{3} \]

ACI 318-11 (Eq. 14-7)

\[ n = \frac{E_c}{E_s} = \frac{29,000}{3,605} = 8.0 > 6.0 \text{ (o.k.)} \]

ACI 318-11 (14.8.3)

Calculate the effective area of longitudinal reinforcement in a slender wall for obtaining an approximate cracked moment of inertia.

\[ A_{se} = A_c + \frac{P_{um} \times h}{2 \times f_y \times d} = 3.08 + \frac{32.0 \times 8.75}{2 \times 60 \times (8.75/2)} = 3.61 \text{ in.}^2 \]

ACI 318-11 (R14.8.3)

The following calculation are performed with the effective area of steel in lieu of the actual area of steel.

\[ a = \frac{A_{se} \times f_y}{0.85 \times f_y \times b} = \frac{3.61 \times 60}{0.85 \times 4 \times (4 \times 12)} = 1.33 \text{ in.} \]

ACI 318-11 (R9.3.2.2)

\[ c = \frac{a}{\beta} = \frac{1.33}{0.85} = 1.56 \text{ in.} \]

\[ \frac{c}{d} = \frac{1.56}{4.375} = 0.356 < 0.375 \therefore \text{ tension-controlled} \]

ACI 318-11 (9.3.2)

\[ \phi = 0.9 \]

\[ I_{cr} = 8.0 \times 3.61 \times (4.375 - 1.56)^2 + \frac{(4 \times 12) \times 1.56^3}{3} = 292 \text{ in.}^3 \]

ACI 318-11 (Eq. 14-7)
\[ M_u = \frac{M_{uw}}{1 - \frac{P_{sw}}{0.75 \times K_b}} \quad \text{ACI 318-11 (Eq. 14-6)} \]

\[ K_b = \frac{48 \times E_c \times I_{cw}}{5 \times t_w^2} = \frac{48 \times 3605 \times 292}{5 \times (29.5 \times 12)^2} = 80.6 \text{ kip} \]

\[ M_u = \frac{14.9}{32.0} = 31.7 \text{ ft-kip} \]

3.3. Tension-controlled verification  
\[ P_n = \frac{P_{sw}}{\phi} = \frac{32.0}{0.9} = 35.5 \text{ kips} \]

\[ a = \frac{A_{cw} \times f_s}{0.85 \times f'_c \times l_w} = \frac{P_n \times h}{2 \times d} + A_i \times f_y = \frac{35.5 \times 8.75}{2 \times 4.375} + 3.08 \times 60 \]

\[ c = \frac{a}{\beta_i} = \frac{1.35}{0.85} = 1.59 \text{ in.} \]

\[ \varepsilon = \left( \frac{0.003}{c} \right) \times d_i - 0.003 = \left( \frac{0.003}{1.59} \right) \times 4.375 - 0.003 = 0.0053 > 0.0050 \]

Therefore, section is tension controlled  
\[ \text{ACI 318-11 (14.8.2.3)} \]

4. Tilt-Up Wall Cracking Moment Capacity (M_{cr})

Determine \( f_c \) = Modulus of rupture of concrete and \( I_c \) = Moment of inertia of the gross uncracked concrete section to calculate \( M_{cr} \)

\[ f_c = 7.5 \lambda \sqrt{f'_c} = 7.5 \times 1.0 \times \sqrt{4,000} = 474.3 \text{ psi} \quad \text{ACI 318-11 (Eq. 9-10)} \]

\[ I_c = \frac{h^3}{12} = \frac{(4 \times 12) \times 8.75^3}{12} = 2680 \text{ in.}^4 \]

\[ y_t = \frac{h}{2} = \frac{8.75}{2} = 4.375 \text{ in.} \]

\[ M_{cr} = \frac{f_c I_c}{y_t} = \frac{474.3 \times 2680}{4.375} \times \frac{1}{1000} \times \frac{1}{12} = 24.2 \text{ ft-kip} \quad \text{ACI 318-11 (Eq. 9-9)} \]

5. Tilt-Up Wall Flexural Moment Capacity (\( \phi M_n \))

\[ M_n = A_y \times f_y \times \left( d - \frac{a}{2} \right) = 3.61 \times 60 \times \left( 4.375 - \frac{1.35}{2} \right) = 801.4 \text{ in.-kip} = 66.8 \text{ ft-kip} \]

It was shown previously that the section is tension controlled \( \Rightarrow \phi = 0.9 \)
\[ \phi M_a = \phi \times M_a = 0.9 \times 66.8 = 60.4 \text{ ft-kip} > M_a = 31.7 \text{ ft-kip} \quad \text{(o.k.)} \quad \text{ACI 318-11 (14.8.3)} \]

\[ \phi M_n = 60.4 \text{ ft-kip} > M_{cr} = 24.4 \text{ ft-kip} \quad \text{(o.k.)} \quad \text{ACI 318-11 (14.8.2.4)} \]

\[ \Delta_s = \frac{M_a}{0.75 \times K_p} = \frac{31.7 \times 12}{0.75 \times 80.6} = 6.29 \text{ in.} \quad \text{ACI 318-11 (Eq. 14-5)} \]

6. **Tilt-Up Wall Vertical Stress Check**

\[ \frac{P_{um}}{A_y} = \frac{32.0 \times 1000}{8.75 \times (4 \times 12)} = 76.2 \text{ psi} < 0.06 \times f_c = 0.06 \times 4000 = 240 \text{ psi} \quad \text{(o.k.)} \quad \text{ACI 318-11 (14.8.2.6)} \]

7. **Tilt-Up Wall Shear Stress Check**

In-plane shear is not evaluated since in-plane shear forces are not applied in this example. Out-of-plane shear due to lateral load should be checked against the shear capacity of the wall. By inspection of the maximum shear forces \( f \), it can be determined that the maximum shear force is under 5 kip. The wall left leg (the weakest section) has a shear capacity approximately 50 kip and no detailed calculations are required by engineering judgement. (See figure 6 for detailed shear force diagram)

8. **Tilt-Up Wall Mid-Height Deflection (\( \Delta_s \))**

The maximum out-of-plane deflection (\( \Delta_s \)) due to service lateral and eccentric vertical loads, including P\( \Delta \) effects, shall not exceed \( l_c/150 \). Where \( \Delta_s \) is calculated as follows:

\[ \Delta_s = \left\{ \begin{array}{ll}
\frac{2}{3} \Delta_s + \frac{M_a - \frac{2}{3} M_{cr}}{M_a - \frac{2}{3} M_{cr}} \times \left( \Delta_s - \frac{2}{3} \Delta_s \right) & \text{When } M_a > \frac{2}{3} M_{cr} \\
\left( \frac{M_a}{M_{cr}} \right) \Delta_{cr} & \text{When } M_a < \frac{2}{3} M_{cr}
\end{array} \right\} \quad \text{ACI 318-11 (14.8.4)} \]

Where \( M_a \) is the maximum moment at mid-height of wall due to service lateral and eccentric vertical loads including P\( \Delta \) effects.

\[ M_a = M_{sw} + P \Delta_s \]

\[ M_{sw} = \frac{w_i \times l_i^2}{8} + \frac{P_s \times e}{2} = \frac{0.7 \times 27.2}{1.6 \times 5} \times (4 + 5) \times (29.5)^2 + \frac{(4.5) \times 3}{12} = 12.2 \text{ ft-kip} \]

\[ P_s = P_{sl} + \text{wall self-weight} = 4.5 + 15.9 = 20.4 \text{ kip} \]

\[ M_{cr} = \frac{f_c I}{y_i} = 24.2 \text{ ft-kip} \quad \text{(as calculated perviously)} \quad \text{ACI 318-11 (Eq. 9-9)} \]
\[ \Delta_{cr} = \frac{5}{48} \times \frac{M_{cr}}{E' I_g} = \frac{5}{48} \times \frac{24.2 \times 12 \times (29.5 \times 12)^2}{3,605 \times 2680} = 0.392 \text{ in.} \quad \text{ACI 318-11 (Eq. 14-10)} \]

\[ \Delta_s \text{ will be calculated by trial and error method since } \Delta_s \text{ is a function of } M_s \text{ and } M_s \text{ is a function of } \Delta_s. \]

Assume \( M_{sa} < \frac{2}{3} M_{cr} \)

Assume \( \Delta_s = \left( \frac{M_{sa}}{M_{cr}} \right) \Delta_{cr} = \left( \frac{12.2}{24.2} \right) \times 0.392 = 0.198 \text{ in.} \)

\[ M_{sa} = M_{sa} + P \Delta_s = 12.2 \times 12 + 20.4 \times 0.198 = 150.4 \text{ in.-kip} = 12.5 \text{ ft-kip} \]

\[ \Delta_s = \left( \frac{M_{sa}}{M_{cr}} \right) \Delta_{cr} = \frac{12.5}{24.2} \times 0.392 = 0.202 \text{ in.} \quad \text{ACI 318-11 (Eq. 14-9)} \]

No further iterations are required

\[ M_{sa} = 12.5 \text{ ft-kip} < \frac{2}{3} M_{cr} = \frac{2}{3} \times 24.2 = 16.1 \text{ ft-kip} \quad (\text{o.k.}) \]

\[ \Delta_s = 0.202 \text{ in.} < \frac{l_e}{150} = \frac{29.5 \times 12}{150} = 2.36 \text{ in.} \quad (\text{o.k.}) \]

The wall left leg is adequate with 7 #6 vertical reinforcement and 8.75 in. thickness.

**Right Leg Analysis and Design**

Repeating the same process for the right leg (right design strip) leads to the following results:

\( P_{dr} = 5.1 \text{ kip} \) (for the right leg)

\( P_{lr} = 5.3 \text{ kip} \) (for the right leg)

\[ w = 27.2 \text{ lb/ft}^2 \]

\( P_{sr} = 14.6 \text{ kip} \)

\( P_{sr} = 37.9 \text{ kip} \)

\[ w_u = 0.150 \text{ kip/ft} \]

\( M_{sa} = 18.1 \text{ ft-kip} \)

\( A_{sr} = 3.71 \text{ in.}^2 \)

\[ a = 0.91 \text{ in.} \]
c = 1.07 in.

\[ \frac{c}{d} = 0.245 < 0.375 \therefore \text{tension-controlled} \]

\[ I_s = 355 \text{ in.}^4 \]

\[ K_s = 98.2 \text{ kip} \]

\[ M_u = 37.3 \text{ ft-kip} \]

\[ M_{cr} = 36.3 \text{ ft-kip} \]

\[ \phi M_u = 65.5 \text{ ft-kip} > M_u = 37.3 \text{ ft-kip} \ (\text{o.k.}) \]

\[ \phi M_u = 65.5 \text{ ft-kip} > M_{cr} = 36.3 \text{ ft-kip} \ (\text{o.k.}) \]

\[ \Delta_u = 6.08 \text{ in.} \]

\[ \frac{P_{\text{min}}}{A_y} = 60.2 \text{ psi} < 0.06 \times f_c = 240 \text{ psi} \ (\text{o.k.}) \]

\[ M_u = 14.9 \text{ ft-kip} \]

\[ \Delta_{cr} = 0.392 \text{ in.} \]

\[ M_u = 15.2 \text{ ft-kip} < \frac{2}{3} M_{cr} = 24.2 \text{ ft-kip} \ (\text{o.k.}) \]

\[ \Delta_s = 0.164 \text{ in.} < \frac{I_s}{150} = 2.36 \text{ in.} \ (\text{o.k.}) \]

The wall right leg is adequate with 7 #6 vertical reinforcement and 8.75 in. thickness.

9. Analysis and Design of the Section between the Design Strips

For the vertical reinforcement for the section between the design strips, minimum area of steel should be provided as follows:

\[ \rho_{l,\text{min}} = 0.0015 \quad \text{ACI 318-11 (14.3.2)} \]

Try single layer panel reinforcement of 9 #4.

\[ \rho_l = \frac{A_{y,\text{vertical}}}{b \times h} = \frac{9 \times 0.20}{(10 \times 12) \times 8.75} = 0.0017 \quad \text{ACI 318-11 (2.1)} \]

\[ \rho_l = 0.0017 \geq \rho_{l,\text{min}} = 0.0015 \ (\text{o.k.}) \]
\[ s_{t,\text{max}} = \text{smallest of } \left\{ \frac{3 \times h}{18 \, \text{in.}} \right\} = \text{smallest of } \left\{ \frac{3 \times 8.75}{18 \, \text{in.}} \right\} = \text{smallest of } \left\{ \frac{26.25 \, \text{in.}}{18 \, \text{in.}} \right\} = 18 \, \text{in.} \quad \text{ACI 318-11 (7.6.5)} \]

\[ s_{t,\text{provided}} = \frac{10 \times 12}{9} = 13.3 \, \text{in.} \leq s_{t,\text{max}} = 18 \, \text{in.} \quad (\text{o.k.}) \]

10. Horizontal Reinforcement

\[ \rho_{h,\text{min}} = 0.00200 \quad \text{ACI 318-11 (14.3.3)} \]

Try single layer panel reinforcement of 33 #4.

\[ \rho_l = \frac{A_{\text{vertical}}}{b \times h} = \frac{33 \times 0.20}{(31 \times 12) \times 8.75} = 0.00203 \quad \text{ACI 318-11 (2.1)} \]

\[ \rho_h = 0.00203 \geq \rho_{h,\text{min}} = 0.00200 \quad (\text{o.k.}) \]

Additional reinforcement requirements are outlined in \textit{ACI 318-11 (14.3.7)} for header and jambs of openings.

11. Tilt-Up Wall Panel Analysis and Design – \textit{spWall} Software

\textit{spWall} is a program for the analysis and design of reinforced concrete shear walls, tilt-up walls, precast walls and Insulate Concrete Form (ICF) walls. It uses a graphical interface that enables the user to easily generate complex wall models. Graphical user interface is provided for:

- Wall geometry (including any number of openings and stiffeners)
- Material properties including cracking coefficients
- Wall loads (point, line, and area),
- Support conditions (including translational and rotational spring supports)

\textit{spWall} uses the Finite Element Method for the structural modeling, analysis, and design of slender and non-slower reinforced concrete walls subject to static loading conditions. The wall is idealized as a mesh of rectangular plate elements and straight line stiffener elements. Walls of irregular geometry are idealized to conform to geometry with rectangular boundaries. Plate and stiffener properties can vary from one element to another but are assumed by the program to be uniform within each element.

Six degrees of freedom exist at each node: three translations and three rotations relating to the three Cartesian axes. An external load can exist in the direction of each of the degrees of freedom. Sufficient number of nodal degrees of freedom should be restrained in order to achieve stability of the model. The program assembles the global stiffness matrix and load vectors for the finite element model. Then, it solves the equilibrium equations to obtain deflections and rotations at each node. Finally, the program calculates the internal forces and internal moments in each element. At the user’s option, the program can perform second order analysis. In this case, the
program takes into account the effect of in-plane forces on the out-of-plane deflection with any number of openings and stiffeners.

In spWall, the required flexural reinforcement is computed based on the selected design standard (ACI 318-11 is used in this example), and the user can specify one or two layers of wall reinforcement. In stiffeners and boundary elements, spWall calculates the required shear and torsion steel reinforcement. Wall concrete strength (in-plane and out-of-plane) is calculated for the applied loads and compared with the code permissible shear capacity.

For illustration and comparison purposes, the following figures provide a sample of the input modules and results obtained from an spWall model created for the reinforced concrete wall in this example.

![Figure 3 – Defining Loads for Tilt-Up Wall Panel with Opening (spWall)](image)
Figure 4 – Factored Axial Forces Contour Normal to Tilt-Up Wall Panel Design Strips Cross-Sections (spWall)
Figure 5 – Tilt-Up Wall Panel Service Lateral Displacement Contour (Out-of-Plane) (spWall)
Figure 6 – Out-of-plane Shear Diagram (spWall)
Figure 7 – Tilt-Up Wall Panel with Opening Moment Diagram (spWall)
### Figure 8 – Tilt-Up Wall Panel with Opening Displacement at Critical Sections (Service Combinations) *(spWall)*

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<th>Dz</th>
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### Figure 9 – Tilt-Up Wall Panel with Opening Displacement at Critical Sections (Ultimate Combinations) *(spWall)*

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<tr>
<td>393</td>
<td>-5.18e-005</td>
<td>-1.91e-003</td>
<td>-1.65e-001</td>
</tr>
<tr>
<td>394</td>
<td>-3.88e-005</td>
<td>-1.91e-003</td>
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<td>-2.59e-005</td>
<td>-1.91e-003</td>
<td>-1.64e-001</td>
</tr>
<tr>
<td><strong>396</strong></td>
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<td><strong>-1.91e-003</strong></td>
<td><strong>-1.64e-001</strong></td>
</tr>
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<td>397</td>
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<td>-1.91e-003</td>
<td>-1.64e-001</td>
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<td>398</td>
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<td>-1.64e-001</td>
</tr>
<tr>
<td>399</td>
<td>3.88e-005</td>
<td>-1.91e-003</td>
<td>-1.64e-001</td>
</tr>
<tr>
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<td>-1.65e-001</td>
</tr>
<tr>
<td>401</td>
<td>6.47e-005</td>
<td>-1.91e-003</td>
<td>-1.65e-001</td>
</tr>
<tr>
<td>402</td>
<td>7.77e-005</td>
<td>-1.91e-003</td>
<td>-1.66e-001</td>
</tr>
</tbody>
</table>

*Note: The values in the tables represent displacements (Dx, Dy, Dz) in inches (in).*
12. Design Results Comparison and Conclusions

The model shown above was created in spWall taking into account the ACI 318-11 provisions (alternative design method) and ACI 551 recommendations regarding the analysis and design of tilt-up wall panels with openings in order to match the results presented in the reference. In this model the left and right design strips are modeled such that the entire lateral and axial load, including self-weight above the critical section, are distributed to the two strips at each side of the opening. The tributary width for loads was taken as the width of the strip plus one-half the width of the opening. The following table shows the comparison between hand and reference results with spWall model results.

<table>
<thead>
<tr>
<th>Solution</th>
<th>$M_u$ (kip-ft)</th>
<th>$N_u$ (kip)</th>
<th>$D_{z,service}$ (in.)</th>
<th>$D_{z,ultimate}$ (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Design Strip</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Hand</td>
<td>31.70</td>
<td>37.30</td>
<td>32.00</td>
<td>37.90</td>
</tr>
<tr>
<td>Reference</td>
<td>31.70</td>
<td>37.30</td>
<td>32.00</td>
<td>37.90</td>
</tr>
<tr>
<td>spWall</td>
<td>32.07</td>
<td>37.71</td>
<td>32.00</td>
<td>37.88</td>
</tr>
</tbody>
</table>

The results of all the hand calculations and the reference used illustrated above are in agreement with the automated exact results obtained from the spWall program.

12.1. Comparison of Wall Modeling Methods

ACI 318 provides the alternative design method as a simple and accurate option for analysis and design of wall meeting the method conditions. Other methods such as finite element analysis can be used to address wall beyond the limitation
of the alternative design method (cantilevered walls, variable thickness and width, complex boundary conditions, walls with high compressive loads or in-plane lateral loads, etc.) The exact wall geometry and applied loads were modeled using spWall engineering software to investigate the differences between the simplified approximate method and the finite element method. For illustration and comparison purposes, the following figures provide a sample of the results obtained from an spWall model created for the reinforced concrete wall in this example using exact wall geometry and applied loads.

It is important to consider the wind load applied to the door opening and how it must be considered and applied in the model based on the door boundary condition. In this example, the door support reactions are assumed along the left and right side of the door opening. Load is modeled as an equivalent uniform line load applied along the right edge of the left leg and the left side of the right leg. The magnitude of this load is calculated as follows:

\[ W_{\text{door}} = 27.2 \times \frac{10}{2} \times \frac{1}{1000} = 0.136 \text{ kip/ft} \]
Figure 11 – Factored Axial Forces Contour - Exact Geometry and Loads (spWall)
Figure 12 – Tilt-Up Wall Panel Service Lateral Displacement Contour (Out-of-Plane) - Exact Geometry and Loads (spWall)
Figure 13 – Out-of-plane Shear Diagram - Exact Geometry and Loads (spWall)
Figure 14 – Tilt-Up Wall Panel with Opening Moment Diagram – Exact Geometry and Loads (spWall)
Figure 15 – Displacement at Critical Sections – Exact Geometry and Loads (Service Combinations) (spWall)

```
<table>
<thead>
<tr>
<th>Node</th>
<th>Dx</th>
<th>Dy</th>
<th>Dz</th>
</tr>
</thead>
<tbody>
<tr>
<td>211</td>
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<td>-2.73e-003</td>
<td>-1.52e-001</td>
</tr>
<tr>
<td>212</td>
<td>-1.09e-003</td>
<td>-2.76e-003</td>
<td>-1.51e-001</td>
</tr>
<tr>
<td>213</td>
<td>-1.59e-003</td>
<td>-2.77e-003</td>
<td>-1.51e-001</td>
</tr>
<tr>
<td>214</td>
<td>-1.05e-003</td>
<td>-2.81e-003</td>
<td>-1.51e-001</td>
</tr>
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<td>-2.83e-003</td>
<td>-1.51e-001</td>
</tr>
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<td>216</td>
<td>-1.03e-003</td>
<td>-2.93e-003</td>
<td>-1.52e-001</td>
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<td>217</td>
<td>-2.84e-004</td>
<td>-2.62e-003</td>
<td>-1.46e-001</td>
</tr>
<tr>
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<td>-2.46e-003</td>
<td>-1.44e-001</td>
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<tr>
<td>219</td>
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<td>-1.44e-001</td>
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<td>220</td>
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<td>-2.23e-003</td>
<td>-1.43e-001</td>
</tr>
<tr>
<td>221</td>
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<td>-2.25e-003</td>
<td>-1.43e-001</td>
</tr>
<tr>
<td>222</td>
<td>-2.37e-004</td>
<td>-2.15e-003</td>
<td>-1.43e-001</td>
</tr>
<tr>
<td>223</td>
<td>-2.18e-004</td>
<td>-2.07e-003</td>
<td>-1.43e-001</td>
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<tr>
<td>224</td>
<td>-1.99e-004</td>
<td>-1.97e-003</td>
<td>-1.44e-001</td>
</tr>
</tbody>
</table>
```

Figure 16 – Displacement at Critical Sections – Exact Geometry and Loads (Ultimate Combinations) (spWall)

```
<table>
<thead>
<tr>
<th>Node</th>
<th>Dx</th>
<th>Dy</th>
<th>Dz</th>
</tr>
</thead>
<tbody>
<tr>
<td>211</td>
<td>-1.72e-003</td>
<td>-4.12e-003</td>
<td>-5.01e+000</td>
</tr>
<tr>
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<td>-1.66e-003</td>
<td>-4.16e-003</td>
<td>-5.86e+000</td>
</tr>
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<td>213</td>
<td>-1.65e-003</td>
<td>-4.20e-003</td>
<td>-5.80e+000</td>
</tr>
<tr>
<td>214</td>
<td>-1.63e-003</td>
<td>-4.23e-003</td>
<td>-5.95e+000</td>
</tr>
<tr>
<td>215</td>
<td>-1.62e-003</td>
<td>-4.27e-003</td>
<td>-4.95e+000</td>
</tr>
<tr>
<td>216</td>
<td>-1.61e-003</td>
<td>-4.42e-003</td>
<td>-4.96e+000</td>
</tr>
<tr>
<td>217</td>
<td>-4.38e-004</td>
<td>-3.94e-003</td>
<td>-6.72e+000</td>
</tr>
<tr>
<td>218</td>
<td>-4.39e-004</td>
<td>-3.76e-003</td>
<td>-6.62e+000</td>
</tr>
<tr>
<td>219</td>
<td>-4.29e-004</td>
<td>-3.51e-003</td>
<td>-6.65e+000</td>
</tr>
<tr>
<td>220</td>
<td>-3.94e-004</td>
<td>-3.36e-003</td>
<td>-6.63e+000</td>
</tr>
<tr>
<td>221</td>
<td>-3.16e-004</td>
<td>-3.27e-003</td>
<td>-4.63e+000</td>
</tr>
<tr>
<td>222</td>
<td>-3.66e-004</td>
<td>-3.22e-003</td>
<td>-4.63e+000</td>
</tr>
<tr>
<td>223</td>
<td>-3.36e-004</td>
<td>-3.06e-003</td>
<td>-4.64e+000</td>
</tr>
<tr>
<td>224</td>
<td>-3.06e-004</td>
<td>-2.94e-003</td>
<td>-4.66e+000</td>
</tr>
</tbody>
</table>
```
Figure 17 – Tilt-Up Wall Panel with Opening Cross-Sectional Forces – Exact Geometry and Loads (spWall)

<table>
<thead>
<tr>
<th>Solution</th>
<th>M_u (kip-ft)</th>
<th>N_u (kips)</th>
<th>D_z,service (in.)</th>
<th>D_z,ultimate (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Simplified Model</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Approximate Design Strips</td>
<td>32.07</td>
<td>37.71</td>
<td>69.78</td>
<td>0.204</td>
</tr>
<tr>
<td>Complete Model</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Exact Geometry and Loads</td>
<td>---</td>
<td>---</td>
<td>59.88</td>
<td>0.151</td>
</tr>
</tbody>
</table>

Using the complete model with the exact wall geometry and applied loads compared with the simplified model of two equivalent design strips results in:

1. Reduction in the required moment capacity by 14%
2. Reduction in the out-of-plane displacements, at service and ultimate levels by 19% to 23% respectively.

The complete model, as shown in the following figure, displays a complete view of the torsional moment distribution indicating areas of torsional stress concentration at opening edges. This corresponds to the additional reinforcement requirements outlined in **ACI 318-11 (14.3.7)** for header and jambs of openings for improved serviceability.
12.2. Tilt-up Wall Stiffness Reduction

In column and wall analysis, section properties shall be determined by taking into account the influence of axial loads, the presence of cracked regions along the length of the member, and the effect of load duration (creep effects). ACI 318 permits the use of moment of inertia values of 0.70 $I_g$ for uncracked walls and 0.35$I_g$ for cracked walls.

*ACI 318-11 (10.10.4.1)*
In **spWall** program, these effects are accounted for where the user can input reduced moment of inertia using “cracking coefficient” values for plate and stiffener elements to effectively reduce stiffness. Cracking coefficients for out-of-plane (bending and torsion) and in-plane (axial and shear) stiffness can be entered for plate elements. Because the values of the cracking coefficients can have a large effect on the analysis and design results, the user must take care in selecting values that best represent the state of cracking at the particular loading stage. Cracking coefficients are greater than 0 and less than 1.

At ultimate loads, a wall is normally in a highly cracked state. The user could enter a value of out-of-plane cracking coefficient for plates of \( \frac{I_{\text{cracked}}}{I_{\text{gross}}} \) based on estimated values of \( A_s \). After the analysis and design, if the computed value of \( A_s \) greatly differs from the estimated value of \( A_s \), the analysis should be performed again with new values for the cracking coefficients. A factor 0.75 can be also used to reduce the calculated bending stiffness of the concrete section in accordance with ACI 318-11, Chapters 10 and 14. It is intended to account for variations in material properties and workmanship. This reduction factor in bending stiffness should be incorporated by all other alternate design methods to comply with the requirements of ACI 318 as ACI 551 committee stated.

At service loads, a wall may or may not be in a highly cracked state. For service load deflection analysis, a problem should be modeled with an out-of-plane cracking coefficient for plates of \( \frac{I_{\text{effective}}}{I_{\text{gross}}} \).

Based on the previous discussion, the ratio between \( I_c \) and \( I_g \) including the reduction factor (0.75) can be used as the cracking coefficient for the out-of-plane case for the ultimate load combinations. In this example, \( I_c \) and \( I_g \) were found to be equal to 292 in.\(^4\) and 2,680 in.\(^4\) for the left leg (design strip). Thus, the out-of-plane cracking coefficient for ultimate load combinations for the left leg can be found as follows:

\[
\alpha = \frac{0.75 \times I_c}{I_g} = \frac{0.75 \times 292}{2,680} = 0.082
\]

For the service load combinations, it was found that \( M_s \) for the left leg equals to 12.5 ft-kip which is less than \( M_{cr} = 24.2 \text{ ft-kip} \). That means the left leg section is uncracked and the cracking coefficient can be taken equal to 1.
12.3. Comparison of Load Type Effects

During the process of analyzing the tilt-up wall panels, the effect of load type on the wall behavior at the critical section was investigated in terms of out-of-plane deflection at service and ultimate level, required axial capacity, and required out-of-plane moment capacity.

<table>
<thead>
<tr>
<th>Table 3 – Effect of Load Type on the Wall Behavior</th>
</tr>
</thead>
<tbody>
<tr>
<td>Solution</td>
</tr>
<tr>
<td>Actual Joists Point Loads</td>
</tr>
<tr>
<td>Equivalent Uniform Line Load</td>
</tr>
</tbody>
</table>

Using equivalent uniform line load along the section width to represent the actual joists point loads has only a slight effect on the results obtained at the critical section (mid-height of the unbrace wall length). However, modeling point loads to reflect actual behavior and stress distribution is beneficial in cases where there are openings, variable thicknesses, changes in geometry, intermediate supports, and other variations from a simply supported wall with constant width and thickness.

12.4. Cracked Moment of Inertia Calculation Methods

The cracked moment of inertia for tilt-up wall panels can be calculated using different ACI 318 provisions. The following shows the commonly used provisions to calculate the cracked moment of inertia:

1. $0.35 I_g$ for cracked walls and $0.75 I_g$ for uncracked walls

2. When treating the wall as compression member:

$$
(0.80 + 25 \times \frac{A_u}{A_g}) \times \left(1 - \frac{M_u}{P_a \times h} - 0.5 \times \frac{P_u}{P_a} \right) \times I_g \leq 0.875 \times I_g
$$

3. When treating the wall as flexural member:

$$
ACI\ 318-11 (10.4.1)
$$

$$
ACI\ 318-11 (Eq. 10-8)
$$

$$
\begin{align*}
M_i = M_{ci} + M_{di} + M_{ei} + M_{oi} \\
N_i = N_{ci} + N_{di} + N_{ei} + N_{oi}
\end{align*}
$$

$$
\begin{align*}
D_{z, service} = D_{z, service}^{0.80} + D_{z, service}^{0.75} \\
D_{z, ultimate} = D_{z, ultimate}^{0.80} + D_{z, ultimate}^{0.75}
\end{align*}
$$
\[ (0.10 + 25\times \rho ) \times \left( 1.2 - 0.2 \times \frac{b_w}{d} \right) \times I_s \leq 0.5 \times I_g \]  
\textit{ACI 318-11 (Eq. 10-9)}

4. Using the moment magnification procedure for nonsway frames:
\[ \frac{0.2 \times E_c \times I_s + E_s \times I_{sw}}{(1 + \beta_{des}) \times E_c} \]  
\textit{ACI 318-11 (Eq. 10-14)}

5. Using the moment magnification procedure for nonsway frames:
\[ \frac{0.4 \times E_c \times I_s}{(1 + \beta_{des}) \times E_c} \]  
\textit{ACI 318-11 (Eq. 10-15)}

6. Using the alternative design method of slender walls:
\[ n \times A_{sw} \times (d - c)^2 + \frac{I_{sw}}{3} \times c^3 \]  
\textit{ACI 318-11 (Eq. 14-7)}

The fourth equation is used in this example to calculate the cracked moment of inertia for the wall section modeled in spWall. This is intended to match the reference approach using the alternative design method to analyze and design the tilt-up wall panels.

The variation in the magnitude of \( I_{cr} \) has a significant effect on the analysis results and specifically the wall moments and displacement. In the following table a comparison of the resulting values based on variation of the \( I_{cr} \) is shown for information.

<table>
<thead>
<tr>
<th>Method</th>
<th>( I_{cr} ), in.(^4)</th>
<th>Cracking coefficient for spWall user</th>
<th>( M_{uu} ), kip-ft</th>
<th>( D_{z,service} ), in.</th>
<th>( D_{z,ultimate} ), in.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Left</td>
<td>Right</td>
<td>Left</td>
<td>Right</td>
<td>Left</td>
<td>Right</td>
</tr>
<tr>
<td>10.10.4.1</td>
<td>938</td>
<td>1407</td>
<td>0.350</td>
<td>0.350</td>
<td>17.03</td>
</tr>
<tr>
<td>Eq. 10-8</td>
<td>2345</td>
<td>3517</td>
<td>0.875</td>
<td>0.875</td>
<td>15.66</td>
</tr>
<tr>
<td>Eq. 10-9</td>
<td>607</td>
<td>715</td>
<td>0.227</td>
<td>0.178</td>
<td>18.49</td>
</tr>
<tr>
<td>Eq. 10-14</td>
<td>126</td>
<td>159</td>
<td>0.047</td>
<td>0.040</td>
<td>177.67</td>
</tr>
<tr>
<td>Eq. 10-15</td>
<td>133</td>
<td>200</td>
<td>0.050</td>
<td>0.050</td>
<td>109.04</td>
</tr>
<tr>
<td>Eq. 14-7</td>
<td>291</td>
<td>356</td>
<td>0.109</td>
<td>0.088</td>
<td>29.68</td>
</tr>
<tr>
<td>Eq. 14-7 with reduction factor (from 14-6)</td>
<td>218</td>
<td>267</td>
<td>0.081</td>
<td>0.066</td>
<td>32.41</td>
</tr>
</tbody>
</table>

Observation of the values above reveal the necessity to carefully select \( I_{cr} \) value to ensure the wall moment capacity and estimated deflections are calculated with sufficient conservatism ensuring adequate strength and stability.